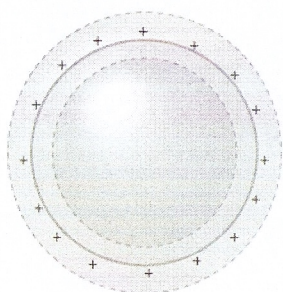


Student 8
 Average 26.1/50
 Best 46/50

12th Physics (2017 – 18)

(3rdQ, #2Mini Test)

Class	No.	Name
		<i>Solutions</i>



In calculation problems, describe equations clearly and systematically enough to show how to solve the problems. If not enough, you won't get any point.

Gravitational acceleration rate	$g = 9.80 \text{ m/s}^2$
Universal Gravitational Constant	$G = 6.67 \times 10^{-11} \text{ N} \cdot \text{m}^2/\text{kg}^2$
Elementary Charge	$e = 1.60 \times 10^{-19} \text{ C}$
Electron Mass	$m_e = 9.11 \times 10^{-31} \text{ kg}$
Proton Mass	$m_p = 1.673 \times 10^{-27} \text{ kg}$
Coulomb's Law Constant	$k = 8.99 \times 10^9 \text{ N} \cdot \text{m}^2/\text{C}^2$
Permittivity of free space	$\epsilon_0 = 8.85 \times 10^{-12} \text{ C}^2/(\text{N} \cdot \text{m}^2)$
Magnetic Permeability of Free Space	$\mu_0 = 4\pi \times 10^{-7} \text{ T} \cdot \text{m/A}$
Avogadro's Number	$N_A = 6.022 \times 10^{23} \text{ mol}^{-1}$
Inch	$1 \text{ in} = 25.4 \text{ mm}$

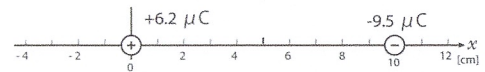
4 pt/question x 13 questions = 52 pt Max 50 pt

/[Total 50 pt]

12thPhysics(2017-18) 3rdQ Quiz-2 *

(1) Two point charges lie on the x axis. A charge of $+6.2 \mu\text{C}$ is at the origin, and a charge of $-9.5 \mu\text{C}$ is at $x = 10.0 \text{ cm}$. What is the net electric field at $x = -4.0 \text{ cm}$.

(Equations)



$$E_A = k \frac{|q_A|}{r_A^2} = k \frac{6.2 \times 10^{-6}}{(4.0 \times 10^{-2})^2}$$

$$E_B = k \frac{|q_B|}{r_B^2} = k \frac{9.5 \times 10^{-6}}{(14.0 \times 10^{-2})^2}$$

$$E_x = -E_A + E_B$$

$$= -k \frac{6.2 \times 10^{-6}}{16 \times 10^{-4}} + k \frac{9.5 \times 10^{-6}}{196 \times 10^{-4}}$$

$$= \frac{(-6.2 \times 196 + 9.5 \times 16) \times 10^{-6}}{16 \times 196 \times 10^{-4}} \times 8.99 \times 10^9$$

$$= -0.3390 \times 10^{-2} \times 8.99 \times 10^9$$

$$= -3.048 \times 10^{-3}$$

$$\rightarrow -3.0 \times 10^{-3}$$

(1) Answer

Direction

To the negative x axis

(48%)

Magnitude $3.0 \times 10^3 \text{ N/C}$

(2) Find the amount of positive electric charge in one mole of lithium atoms.

(Equations)



$$Q = 3 \times N_A \times e$$

$$= 3 \times 6.022 \times 10^{23} \times 1.60 \times 10^{-19}$$

$$= 28.91 \times 10^4$$

$$= 2.891 \times 10^5 \rightarrow 2.89 \times 10^5$$

(2) Answer

$2.89 \times 10^5 \text{ C}$

(31%)

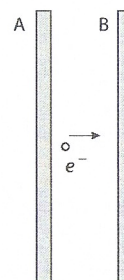
(3) An electron starts from one plate A of a charged closely spaced parallel plate arrangement with an initial velocity of 1.63×10^4 m/s to the right. Its speed on reaching the other plate B, 2.10 cm away is 4.15×10^4 m/s.

(3-a) What type of charge is on each plate?

(3-b) What is the direction of the electric field between the plates?

(3-c) If the plates are square with an edge length of 25.4 cm, determine the charge on each.

(Equations)



$$Q = \sigma A \quad \text{--- (1)}$$

$$\text{Gauss' Law } E = \frac{\sigma}{\epsilon_0} \quad \text{--- (2)}$$

$$\Delta V = E/d \quad \text{--- (3)}$$

$$e\Delta V = \Delta K = \frac{me}{2} (v_B^2 - v_A^2) \quad \text{--- (4)}$$

$$Q = \sigma A$$

$$= A \epsilon_0 E$$

$$= A \epsilon_0 d \Delta V$$

$$= \frac{A \epsilon_0 d me}{2e} (v_B^2 - v_A^2)$$

$$= \frac{(25.4 \times 10^{-2})^2 \times 8.85 \times 10^{-12} \times 2.10 \times 10^{-2} \times 9.11 \times 10^{-31}}{2 \times 1.60 \times 10^{-19}} (4.15^2 - 1.63^2) \times 10^8$$

$$= 4.972 \times 10^5 \times 10^{-4-12-2-31+8+19}$$

$$= 4.972 \times 10^{-17} \rightarrow 4.97 \times 10^{-17} \text{ (C)}$$

(3-a) Answer

A: negative

B: positive

(3-b) Answer

From B to A

(48%)

(3-c) Answer

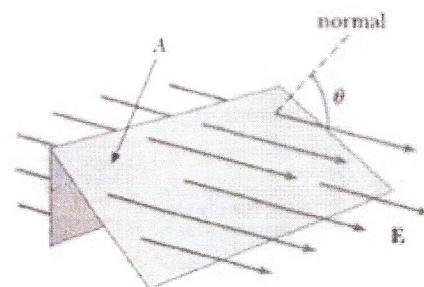
$4.97 \times 10^{-17} \text{ C}$

(4) A flat sheet of paper of area 0.250 m^2 is oriented so that the normal to the sheet at an angle of 60.0° to a uniform electric field of magnitude of 14.0 N/C . Find the magnitude of the electric flux through the sheet.
(Equations)

$$\Phi = EA \cos \theta$$

$$= 14.0 \times 0.250 \times \cos 60.0^\circ$$

$$= 1.750 \rightarrow 1.75$$



(4) Answer

$$1.75 \text{ N}\cdot\text{m}^2/\text{C}$$

(59%)

(5) Rank the Gaussian surfaces shown in the figure in order of increasing electric flux, using the signs, <, = and >.

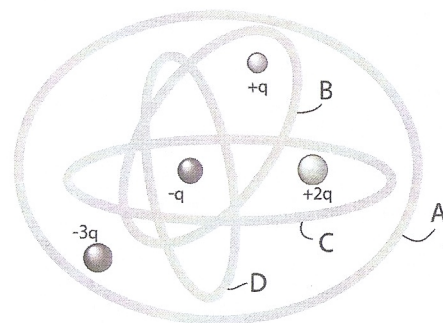
$$A: -3 + 2 + 1 - 1 = -1$$

$$B: 1 - 1 = 0$$

$$C: +2 - 1 = 1$$

$$D: -1$$

$$\Phi = \frac{\text{enclosed charge}}{\epsilon_0}$$



(5) Answer

$$A = D < B < C$$

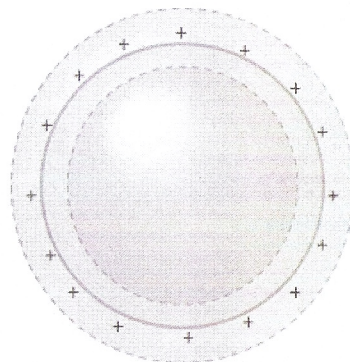
(81%)

(6,7) A solid metal sphere of radius 0.450m carries a net charge of 0.250nC.

(6) Find the magnitude of the electric field at a point 0.100 m outside the surface of the sphere.

(7) Find the magnitude of the electric field at a point inside the sphere, 0.100m below the surface.

(Equations)



(6)

$$\Phi = EA$$

$$\Phi = \frac{q}{\epsilon_0}$$

$$\therefore E = \frac{q}{A \epsilon_0} = \frac{q}{4\pi r^2 \cdot \epsilon_0}$$

$$= \frac{0.250 \times 10^{-9}}{8.85 \times 10^{-12} \times 4\pi \times (0.450 + 0.100)^2}$$

$$= 7.430 \times 10^{-3} \times 10^{-9+12}$$

$$= 7.430 \times 10^{-3+3} \rightarrow 7.43$$

7.43

(7)

$$\Phi = EA = \frac{q}{\epsilon_0}, \quad q = 0$$

$$\therefore E = 0$$

(6) Answer

7.43 N/C

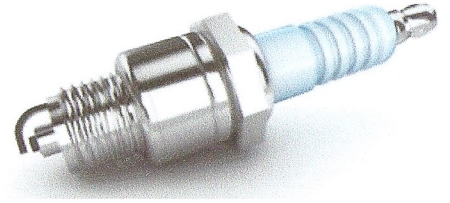
(56%)

(7) Answer

0

(38%)

(8) A spark plug in a car has electrodes separated by a gap of 0.025 in. To create a spark and ignite the air-fuel mixture in the engine, an electric field of 3.0×10^6 N/C is required in the gap. What potential difference must be applied to the spark plug to initiate a spark?
(Equations)

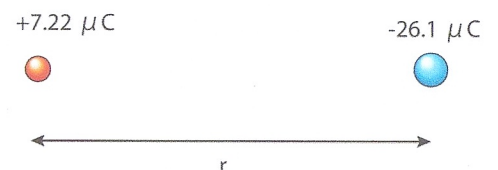


$$\begin{aligned}\Delta V &= E d \\ &= 3.0 \times 10^6 \times 0.025 \times 25.4 \times 10^{-3} \\ &= 1.905 \times 10^3 \text{ (V)} \\ &= 1.905 \text{ kV} \\ &\rightarrow 1.9 \text{ kV}\end{aligned}$$

(8) Answer

1.9 kV (66%)

(9) How far must the point charges $q_1 = +7.22 \mu\text{C}$ and $q_2 = -26.1 \mu\text{C}$ be separated for the electric potential energy of the system to be -126 J ?
(Equations)



$$\begin{aligned}U &= 8.99 \times 10^9 \times \frac{q_1 q_2}{r} \\ \rightarrow r &= \frac{8.99 \times 10^9 \times 7.22 \times 10^{-6} \times (-26.1) \times 10^{-6}}{-126} \\ &= 13.45 \times 10^{-3} \\ &= 1.345 \times 10^{-2} \text{ (m)} \\ &= 1.345 \text{ (cm)} \\ &\rightarrow 1.34 \text{ cm}\end{aligned}$$

(9) Answer

1.34 cm (44%)

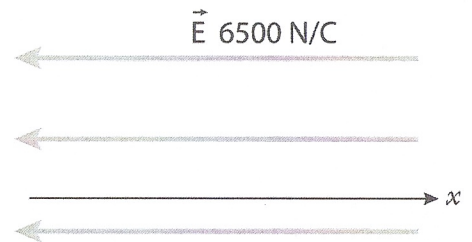
(10) Consider a region in space where a uniform electric field $E = 6500$ N/C points in the negative x direction.

(10-a) What is the orientation of the equipotential surface?

(10-b) If you move in the positive x direction, does the electric potential increase or decrease?

(10-c) What is the distance between the $+14$ -V and the $+16$ -V equipotentials?

(Equations)



$$E = 6500 \text{ N/C} = 6500 \text{ V/m}$$

$$\frac{6500 \text{ V}}{1 \text{ m}} = \frac{(16-14) \text{ V}}{x}$$

$$x = \frac{2}{6500} (\text{m})$$

$$= 0.308 (\text{mm})$$

$$\rightarrow 0.31 \text{ mm}$$

(10-a) Answer

Perpendicular to the
 x axis

(10-b) Answer

Increase

(53%)

(10-c) Answer

0.31 mm

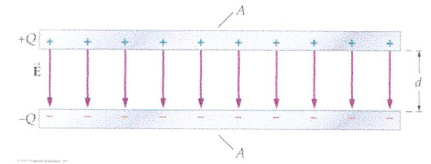
(11~13) A parallel-plate capacitor is constructed with plates of area 0.0590 m^2 and separation 0.550 mm .

(11) Find the magnitude of the charge on each plate of this capacitor when the potential difference between the plates is 32.8 V .

(12) What is the magnitude of the electric field between the plates of the capacitor?

(13) Next, the space between the plates is filled with a dielectric with relative permittivity $\epsilon_r (= \kappa)$. When the capacitor is connected to a 32.8 V battery, each of the plates has a charge of magnitude $2.11 \times 10^{-7} \text{ C}$. What is the value of the ϵ_r ?

(Equations)



$$(11) \quad E = \frac{\sigma}{\epsilon_0} = \frac{Q}{\epsilon_0 A}, \quad E = \frac{V}{d}$$

$$\begin{aligned} \therefore Q &= \frac{V}{d} \cdot \frac{\epsilon_0 A}{1} \\ &= \frac{32.8 \times 8.85 \times 10^{-12} \times 0.0590}{0.550 \times 10^{-3}} \\ &= 31.14 \times 10^{-12+3} = 31.14 \times 10^{-9} = 3.114 \times 10^{-8} \rightarrow 3.11 \times 10^{-8} \end{aligned}$$

$$(12) \quad E = \frac{V}{d} = \frac{32.8}{0.550 \times 10^{-3}} = 59.64 \times 10^3 \text{ (N/C)} = 5.963 \times 10^4 \rightarrow 5.96 \times 10^4$$

(13)

$$C' = \epsilon_r C$$

$$C = \epsilon_0 \frac{A}{d}$$

$$C' = \frac{Q'}{V}$$

$$\therefore \epsilon_r = \frac{C'}{C} = \frac{\frac{Q'}{V}}{\epsilon_0 \frac{A}{d}} = \frac{Q' d}{\epsilon_0 A V}$$

$$= \frac{2.11 \times 10^{-7} \times 0.550 \times 10^{-3}}{8.85 \times 10^{-12} \times 0.0590 \times 32.8}$$

$$\begin{aligned} &= 0.06778 \times 10^{-10+12} = 6.778 \\ &\rightarrow 6.78 \end{aligned}$$

(11) Answer

$$3.11 \times 10^{-8} \text{ C} \quad (56\%)$$

(12) Answer

$$5.96 \times 10^4 \text{ V/m} \quad (48\%)$$

(13) Answer

$$6.78 \quad (36\%)$$