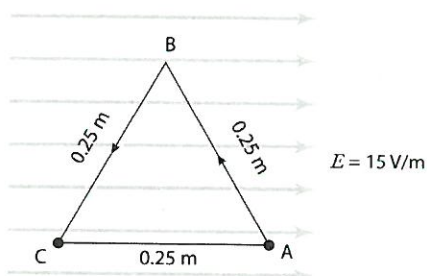


Student 8  
 Average 40.8/100  
 Best 82.0/100

12<sup>th</sup>G Physics (2018– 19)3<sup>rd</sup> Q Exam

(March 21, 2019)

Class	No.	Name <i>Solutions</i>
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In a calculation problem, describe equations clearly and systematically enough to show how to solve the problem. If not enough, you won't get any points.

5point/question x 21questions=105points  
 Max 100 points

Exam

/[Total 100 点]

Lab Reports

Homework

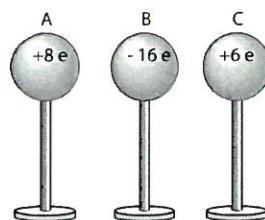
Gravitational acceleration rate	$g = 9.80 \text{ m/s}^2$
Atmospheric Pressure	$1.00 \text{ atm} = 1.013 \times 10^5 \text{ Pa}$
Avogadro's Number	$N_A = 6.022 \times 10^{23} \text{ molecule / mol}$
Universal Gas Constant	$R = 8.31 \text{ J/(mol} \cdot \text{K)}$
Boltzmann Constant	$k = 1.38 \times 10^{-23} \text{ J/K}$
Elementary Charge	$e = 1.60 \times 10^{-19} \text{ C}$
Electron Mass	$m_e = 9.11 \times 10^{-31} \text{ kg}$
Proton Mass	$m_p = 1.673 \times 10^{-27} \text{ kg}$
Coulomb's Law Constant	$k = 8.99 \times 10^9 \text{ N} \cdot \text{m}^2/\text{C}^2$
Permittivity of Free Space	$\epsilon_0 = 8.85 \times 10^{-12} \text{ C}^2/(\text{N} \cdot \text{m}^2)$
Universal Gravitational Constant	$G = 6.67 \times 10^{-11} \text{ N} \cdot \text{m}^2/\text{kg}^2$
Avogadro's Number	$N_A = 6.022 \times 10^{23} \text{ mol}^{-1}$
Magnetic Permeability of Free Space	$\mu_0 = 4\pi \times 10^{-7} \text{ T} \cdot \text{m/A}$

(1) The diagram shows the initial charges and positions of three metal spheres, A, B and C on insulating stands. A is brought into contact with B and then removed. Then B is brought into contact with C and removed. What is the charge on C?

(Equations)

$$\frac{+8 - 16}{2} = \frac{-8}{2} = -4$$

$$\frac{-4 + 6}{2} = \frac{2}{2} = 1$$



(1) Answer

+ 1 e

36%

(2) Find the total electric charge of 1.5 kg of protons.

(Equations)

$$1.5 \text{ kg} \times \frac{1 \text{ proton}}{1.673 \times 10^{-27} \text{ kg}} \times \frac{1.60 \times 10^{-19} \text{ C}}{1 \text{ proton}}$$

$$= 1.435 \times 10^8 \text{ (C)}$$

$$\rightarrow 1.4 \times 10^8 \text{ C}$$

(2) Answer

$1.4 \times 10^8 \text{ C}$

63%

(3) The attractive electrostatic force between the point charges  $+8.44 \times 10^{-6} \text{ C}$  and  $Q$  has a magnitude of  $0.975 \text{ N}$  when the separation between the charges is  $1.31 \text{ m}$ . Find the sign and magnitude of the charge  $Q$ .

(Equations)

$$\begin{aligned}
 F &= k \frac{|q_1 q_2|}{r^2} \\
 |Q| &= \frac{F r^2}{k q} \\
 &= \frac{0.975 \times 1.31^2}{8.99 \times 10^9 \times 8.44 \times 10^{-6}} \\
 &= 0.022052 \times 10^{-3} \\
 &\rightarrow 2.21 \times 10^{-5} \text{ C}
 \end{aligned}$$

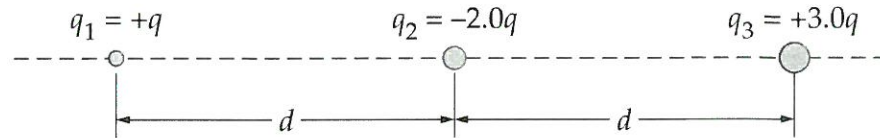
(3) Answer

$$-2.21 \times 10^{-5} \text{ C}$$

64 %

(4) Given that  $q = +12.1 \mu\text{C}$  and  $d = 16 \text{ cm}$ , find the direction and magnitude of the net electrostatic force exerted on the point charge  $q_1$  in the figure.

(Equations)



$$F_3 \leftarrow \bigcirc \rightarrow F_2$$

$$F = F_2 - F_3$$

$$= k \frac{181281}{d^2} - k \frac{8.38}{(2d)^2} = \frac{2k8^2}{d^2} - \frac{3k8^2}{4d^2}$$

$$= \frac{k8^2}{d^2} \left(2 - \frac{3}{4}\right)$$

$$= \frac{8.99 \times 10^9 \times 12.1^2 \times 10^{-12} \times \frac{5}{4}}{0.16^2}$$

$$= 64269 \times 10^{-3}$$

$$= 6.4269 \times 10^1 \rightarrow 64 \text{ N}$$

(4) Answer

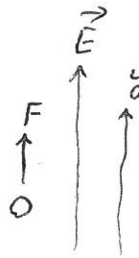
64 N

49%

(5) A  $+5.0 \mu\text{C}$  charge experiences a  $0.44\text{N}$  force in the positive  $y$  direction. If this charge is replaced with a  $-2.7 \mu\text{C}$  charge, what force will it experience?

(Equations)

$$E = \frac{F}{q} = \frac{0.44}{5 \times 10^{-6}} \text{ [N/C]} \quad +5.0 \mu\text{C}$$



$$F' = q' E$$

$$= -2.7 \times 10^{-6} \times \frac{0.44}{5 \times 10^{-6}}$$

$$= -0.238 \rightarrow -0.24 \text{ [N]}$$

(5) Answer  
 $-0.24 \text{ N}$   
 negative  $y$

73%

(6) Referring to the figure, suppose  $q_2$  is not known. Instead, it is given that  $q_1 + q_2 = -2.5 \mu\text{C}$ . Find  $q_1$ ,  $q_2$ , and  $q_3$ .

(Equations)

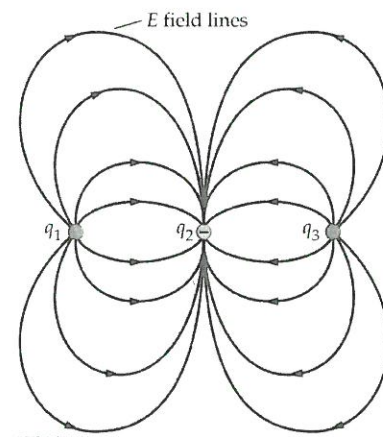
$$q_1 = q_3$$

$$q_2 = -2q_1$$

$$q_1 + q_2 = -2.5 \rightarrow q_1 - 2q_1 = -2.5$$

$$\rightarrow q_1 = 2.5$$

$$q_2 = -2 \times 2.5 = -5.0$$



$$q_1 = +2.5 \mu\text{C}$$

$$q_2 = -5.0 \mu\text{C}$$

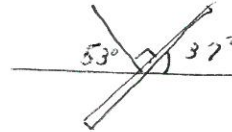
$$q_3 = +2.5 \mu\text{C}$$

24%

(7) A uniform electric field of magnitude 25,000 N/C makes an angle of  $37^\circ$  with a plane surface of area  $0.0153 \text{ m}^2$ . What is the electric flux through this surface?

(Equations)

$$\Phi = EA \cos \theta$$



$$\begin{aligned}\Phi &= 25000 \times 0.0153 \cos 53^\circ \\ &= 230.2\end{aligned}$$

(7) Answer

$$230 \text{ N}\cdot\text{m}^2/\text{C}$$

64%

(8) When an ion accelerates through a potential difference of 2140 V, its electric potential energy decreases by  $1.37 \times 10^{-15} \text{ J}$ . What is the valence of the ion?

(Equations)

$$U = qV$$

$$q = \frac{U}{V} = \frac{1.37 \times 10^{-15}}{2140}$$

$$\frac{q}{e} = \frac{1.37 \times 10^{-15}}{2140 \times 1.60 \times 10^{-19}} = 4.00$$

(8) Answer

$$\pm 4$$

40%

(9) The electrons in a TV picture tube are accelerated from rest through a potential difference of 25 kV. What is the speed of the electrons after they have been accelerated by this potential difference?

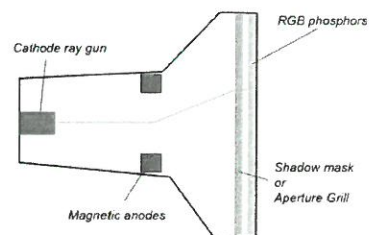
(Equations)

$$eV = \frac{1}{2} m v^2$$

$$v = \sqrt{\frac{2eV}{m}}$$

$$= \sqrt{\frac{1.60 \times 25 \times 2 \times 10^{-16}}{9.11 \times 10^{-31}}} = \sqrt{8.78 \times 10^{15}} = \sqrt{87.8 \times 10^7}$$

$$= 9.37 \times 10^7 \rightarrow 9.4 \times 10^7 \text{ m/s}$$

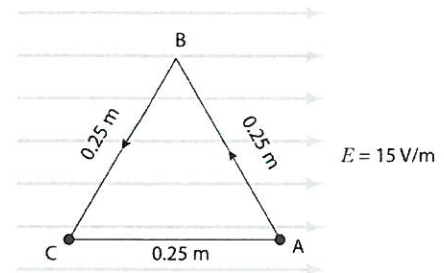


(9) Answer

$$9.4 \times 10^7 \text{ m/s}$$

40%

(10) An electron is moved from point A to point B and then to point C along two legs of an equilateral triangle with sides of length 0.25 m, as shown in the figure. The horizontal electric field is 15 V/m.



(10-a) What is the magnitude of the work required?

(10-b) What is the potential difference between points A and C?

(10-c) Which point is at a higher potential?

(Equations)

$$E = 15 \text{ V/m}$$

$$(a) V = Ed = 15 \times 0.25 \text{ [V]}$$

$$W = qV = -1.60 \times 10^{-19} \times 15 \times 0.25 \\ = -6.00 \times 10^{-19} \text{ [J]}$$

(b)

$$V = 15 \times 0.25 = 3.75 \rightarrow 3.8 \text{ [V]}$$

(c)

(10-a) Answer
$-6.0 \times 10^{-19} \text{ J}$
(10-b) Answer
$3.8 \text{ V}$
(10-c) Answer
C

48%



(11) Consider a region in space where a uniform electric field  $E = 6500 \text{ N/C}$  in the negative  $x$  direction.

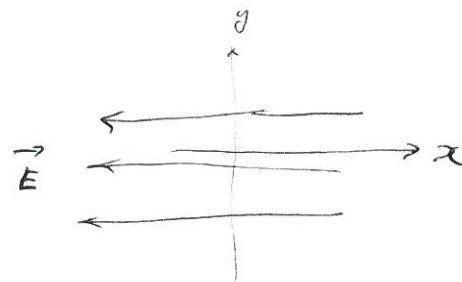
(11-a) What is the orientation of the equipotential surfaces?

Choose one from the followings: parallel to the  $yz$  plane; parallel to the  $xz$  plane; parallel to the  $xy$  plane.

(11-b) If you move in the positive  $x$  direction, does the electric potential increase or decrease?

(11-c) What is the distance between the  $+14\text{-V}$  and the  $+16\text{-V}$  equipotentials?

(Equations)



(a)

(b)

(c) 
$$\frac{16 - 14}{x} = 6500 \text{ V/m}$$

$$x = \frac{2}{6500} = 3.08 \times 10^{-4} \rightarrow 3 \times 10^{-4} \text{ (m)}$$

(11-a) Answer	parallel to $yz$ plane
(11-b) Answer	decreases
(11-c) Answer	$3 \times 10^{-4} \text{ m}$

54%

(12) A parallel-plate capacitor is constructed with circular plates of radius 0.056 m. The plates are separated by 0.25 mm, and the space between the plates is filled with a dielectric with dielectric constant  $\epsilon_r$ . When the charge on the capacitor is  $1.2 \mu\text{C}$  the potential difference between the plates is 750 V. Find the value of the dielectric constant  $\epsilon_r$ .

(Equations)

$$r = 0.056 \text{ m}$$

$$V = 750 \text{ V}$$

$$C = \epsilon_r \epsilon_0 \frac{A}{d}, \quad Q = CV$$

$$\frac{Q}{V} = \epsilon_r \epsilon_0 \frac{A}{d}$$

$$\epsilon_r = \frac{Q d}{V \epsilon_0 A}$$

$$= \frac{1.2 \times 10^{-6} \times 0.25 \times 10^{-3}}{750 \times 8.85 \times 10^{-12} \times \pi \times 0.056^2}$$

$$= 0.004590 \times 10^{-9+12}$$

$$= 4.590 \rightarrow 4.6$$

(12) Answer

4.6

35%

(13) A  $0.22\text{-}\mu\text{F}$  capacitor is charged by a  $1.5\text{-V}$  battery. After being charged, the capacitor is connected to a small electric motor. Assume 100% efficiency.

(13-a) To what height can the motor lift a  $5.0\text{-g}$  mass?

(13-b) What initial voltage must the capacitor have if it is to lift a  $5.0\text{-g}$  mass through a height of  $1.0\text{ cm}$ ?

(Equations)

$$\begin{aligned}
 (a) \quad U &= \frac{1}{2} C V^2 \\
 U &= mgh \quad ) \quad mgh = \frac{1}{2} C V^2 \\
 h &= \frac{C V^2}{2mg} = \frac{0.22 \times 10^{-6} \times 1.5^2}{2 \times 5 \times 10^{-3} \times 9.80} \\
 &= 5.0505 \times 10^{-6} \rightarrow 5.1 \times 10^{-6} \text{ m}
 \end{aligned}$$

$$\begin{aligned}
 (b) \quad V &= \sqrt{\frac{2mgh}{C}} = \sqrt{\frac{2 \times 5 \times 10^{-3} \times 9.80 \times 10^{-2}}{0.22 \times 10^{-6}}} \\
 &= \sqrt{4450} = 66.7 \rightarrow 67
 \end{aligned}$$

(13-a) Answer

$5.1 \mu\text{m}$

(13-b) Answer

$67 \text{ V}$

21%

(14) The four conducting cylinders shown in the figure are all made of the same material, though they differ in length and/or diameter. They are connected to four different batteries, which supply the necessary voltages to give the circuits the same current,  $I$ . Rank the four voltages,  $V_1$ ,  $V_2$ ,  $V_3$ , and  $V_4$ , in order of increasing value. Indicate ties using the sign of  $>$ .

(Equations)

$$R_1 = \rho \frac{3L}{\pi D^2} = \frac{\rho L}{\pi D^2} \cdot 4$$

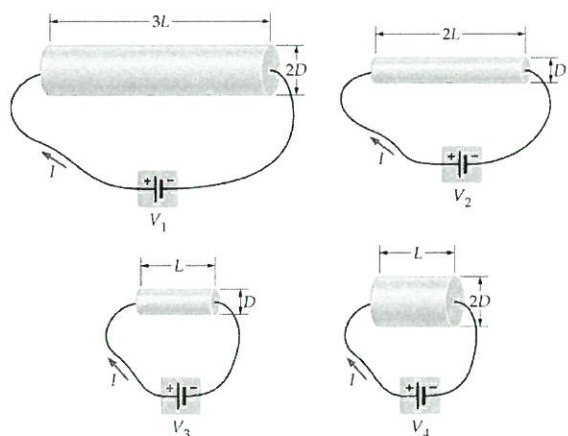
$$R_2 = \rho \frac{2L}{\pi \left(\frac{D}{4}\right)^2} = " \cdot 8$$

$$R_3 = \rho \frac{L}{\pi \left(\frac{D}{4}\right)^2} = " \cdot 4$$

$$R_4 = \rho \frac{L}{\pi D^2} = " \cdot 1$$

$$R_4 < R_1 < R_3 < R_2$$

$$V = IR$$



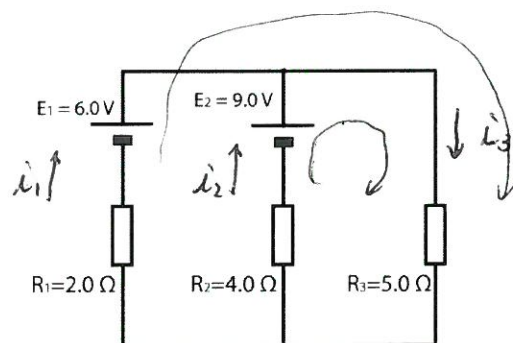
(14) Answer

$$V_4 < V_1 < V_3 < V_2$$

38%

(15) Two batteries and three resistors are connected as shown in the figure. How much current flows through each battery?

(Equations)



$$i_3 = i_1 + i_2 \quad \text{--- ①}$$

$$6 = 2i_1 + 5i_3 \quad \text{--- ②}$$

$$9 = 4i_2 + 5i_3 \quad \text{--- ③}$$

$$6 = 2i_1 + 5i_1 + 5i_2 = 7i_1 + 5i_2 \quad \text{--- ②'}$$

$$9 = 4i_2 + 5i_1 + 5i_2 = 5i_1 + 9i_2 \quad \text{--- ③'}$$

$$\begin{array}{r} 54 = 63i_1 + 45i_2 \\ \rightarrow 45 = 25i_1 + 45i_2 \end{array}$$

$$9.0 = 38i_1$$

$$i_1 = 0.237$$

$$\begin{aligned} \text{②}' \rightarrow i_2 &= \frac{6 - 7i_1}{5} \\ &= \frac{6 - 7 \times 0.237}{5} = 0.868 \end{aligned}$$

$$i_3 = i_1 + i_2 = 1.105$$

(15) Answer

E1 0.24 A

E2 0.87 A

40%

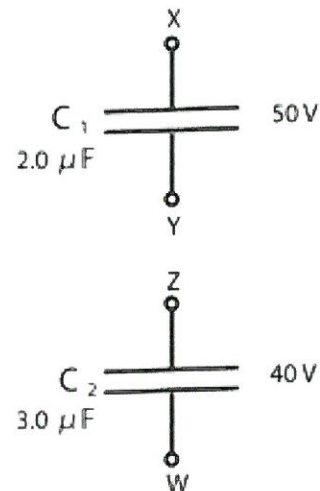
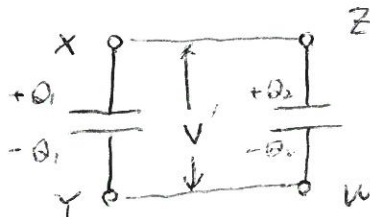
(16, 17) Two capacitors,  $C_1$  and  $C_2$ , with capacitances of  $2.0 \mu\text{F}$  and  $3.0 \mu\text{F}$ , respectively are charged with  $50 \text{ V}$  and  $40 \text{ V}$ , respectively. X and Z are positive electrodes while Y and W are negative ones. Find the electric potential between the plates and the charge on  $C_1$  in the following two cases:

(16) In the case where X is connected with Z, and Y is connected with W.

(17) In the case where X is connected with W, and Y is connected with Z.

(Equations)

(a)



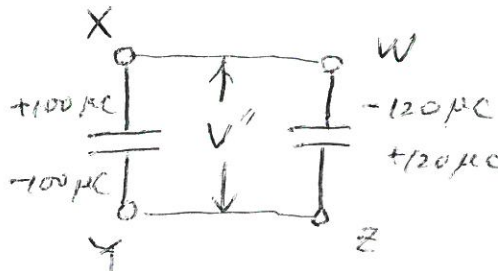
$$Q_1 = C_1 V_1 = 2.0 \mu\text{F} \times 50 = 100 \mu\text{C}$$

$$Q_2 = C_2 V_2 = 3.0 \mu\text{F} \times 40 = 120 \mu\text{C}$$

$$C_1 V' + C_2 V' = 220 \mu\text{C} \quad V' = \frac{220 \mu\text{C}}{2.0 \mu\text{F} + 3.0 \mu\text{F}} = 44.0 \text{ (V)}$$

$$Q'_1 = C_1 V' = 2.0 \mu\text{F} \times 44.0 = 88 \mu\text{C}$$

(b)



$$C_1 V'' + C_2 V'' = 100 \mu\text{C} - 120 \mu\text{C}$$

$$V'' = \frac{-20 \mu\text{C}}{2.0 \mu\text{F} + 3.0 \mu\text{F}} = -4.0 \text{ V}$$

$$\text{potential} = 4.0 \text{ V}$$

$$Q''_1 = C_1 V'' = 2.0 \mu\text{F} \times 4.0 = 8.0 \mu\text{C}$$

(16) Answer

$$44 \text{ V}$$

$$88 \mu\text{C}$$

13%

(17) Answer

$$4.0 \text{ V}$$

$$8.0 \mu\text{C}$$

13%

(18) An electron accelerated from rest through a voltage of 550 V enters a region of constant magnetic field. If the electron follows a circular path with a radius of 17 cm, what is the magnitude of the magnetic field?

(Equations)

$$eV = \frac{1}{2}mv^2 \rightarrow v = \sqrt{\frac{2eV}{m}}$$

$$qB = m \frac{v}{r}$$

$$B = \frac{mv}{er} = \frac{m}{er} \sqrt{\frac{2eV}{m}} = \frac{1}{r} \sqrt{\frac{2mV}{e}}$$

$$= \frac{1}{0.17} \sqrt{\frac{2 \times 9.11 \times 10^{-31} \times 550}{1.60 \times 10^{-19}}}$$

$$= \frac{1}{0.17} \sqrt{6263 \times 10^{-12}}$$

$$= \frac{79.14}{0.17} \times 10^{-6}$$

$$= 466 \times 10^{-6} \rightarrow 4.7 \times 10^{-4} \text{ (T)}$$

(18) Answer

$$4.7 \times 10^{-4} \text{ T}$$

16%

(19) A  $6.60 \mu\text{C}$  particle moves through a region of space where an electric field of magnitude  $1250 \text{ N/C}$  points in the positive  $x$  direction, and a magnetic field of magnitude  $1.02 \text{ T}$  points in the positive  $z$  direction. If the net force acting on the particle is  $6.23 \times 10^{-3} \text{ N}$  in the positive  $x$  direction, find the magnitude and direction of the particle's velocity.

(Equations)

+ charge to positive  $y$

$$F_E = qE$$

$$F_B = qvB$$

$$F = F_E + F_B = qE + qvB$$

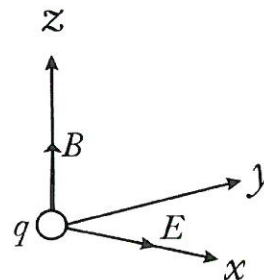
$$v = \frac{F - qE}{qB}$$

$$= \frac{6.23 \times 10^{-3} - 6.60 \times 10^{-6} \times 1250}{6.60 \times 10^{-6} \times 1.02}$$

$$= \frac{(6.23 - 8.25) \times 10^{-3}}{6.732 \times 10^{-6}}$$

$$= -0.3001 \times 10^3$$

$$\rightarrow -300 \text{ [m/s]}$$



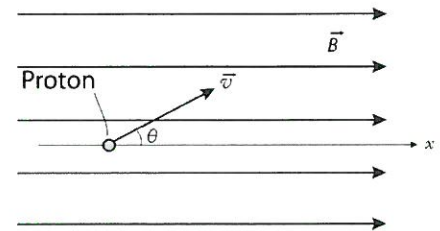
(19) Answer

300 m/s  
to negative  $y$

26%



(20-21) A proton is sent with a speed of  $1.05 \times 10^5$  m/s into a uniform magnetic field of 0.750 T at an angle  $\theta = 30.0^\circ$  as shown in the figure.



(20) Find the period of the spiral movement of the proton.

(21) Find the distance the particle travels in the direction of the magnetic field during one cycle.

(Equations)

$$v_x = v \cos \theta = 1.05 \times 10^5 \cos 30^\circ$$

$$v_y = v \sin \theta = 1.05 \times 10^5 \sin 30^\circ$$

$$q v_y B = m \frac{v_y^2}{r} \rightarrow \frac{r}{v_y} = \frac{m}{q B} \quad \text{--- (1)}$$

$$T = \frac{2\pi r}{v_y} \quad \text{--- (2)} \quad \text{①, ②} \rightarrow T = \frac{2\pi m}{q B}$$

$$\text{①, ②} \quad T = \frac{2\pi m}{q B} = \frac{2\pi \times 1.673 \times 10^{-27}}{1.60 \times 10^{-19} \times 0.750} = 8.761 \times 10^{-27+19} \rightarrow 8.76 \times 10^{-8} \text{ s}$$

$$\begin{aligned} x = v_x t &= 1.05 \times 10^5 \cos 30^\circ \times 8.761 \times 10^{-8} \\ &= 7.967 \times 10^{-3} \text{ [m]} \end{aligned}$$

(20) Answer

$$8.76 \times 10^{-8} \text{ s}$$

43%

(21) Answer

$$7.97 \times 10^{-3} \text{ m}$$

19%

Your opinions

The solution will be shown on the Website of Physic Class tomorrow night.