

Ball Bounding on a floor infinite times

10-23, 2015 Tohei Moritani

$$e = \sqrt{\frac{h_{n+1}}{h_n}} \rightarrow h_{n+1} = h_n e^2$$

$$h = \frac{1}{2} g t^2 \rightarrow t = \sqrt{\frac{2h}{g}}$$

$$T_0 = \sqrt{\frac{2h_0}{g}}$$

$$h_1 = h_0 e^2 \quad T_1 = 2 \sqrt{\frac{2h_1}{g}} = 2 e \sqrt{\frac{2h_0}{g}}$$

$$h_2 = h_1 e^2 = h_0 e^4 \quad T_2 = 2 \sqrt{\frac{2h_2}{g}} = 2 e^2 \sqrt{\frac{2h_0}{g}}$$

$$h_3 = h_2 e^2 = h_0 e^6 \quad T_3 = 2 \sqrt{\frac{2h_3}{g}} = 2 e^3 \sqrt{\frac{2h_0}{g}}$$

$$h_n = h_{n-1} e^2 = h_0 e^{2n} \quad T_n = 2 \sqrt{\frac{2h_n}{g}} = 2 e^n \sqrt{\frac{2h_0}{g}}$$

$$k = 2 \sqrt{\frac{2h_0}{g}}$$

$$\text{Total Time} = \frac{k}{2} + k (e + e^2 + e^3 + \dots e^n)$$

$$\text{When } e < 1, \quad \lim_{n \rightarrow \infty} \sum_{n=0}^{\infty} e^n = \frac{1}{1-e}$$

$$\therefore \text{Total Time} = k \left(\frac{1}{1-e} - \frac{1}{2} \right)$$

$$h_0 = 1.00 \text{ m}, \quad e = 0.800, \quad v_0 = 1.00 \text{ m/s}$$

$$k = 2 \sqrt{\frac{2 \times 1}{9.8}} = 0.9035$$

$$\text{Total Time} = 0.9035(5 - 0.5) = 4.068$$

$$\underline{\text{Total Time } 4.07 \text{ s}, \text{Total Distance } 4.07 \text{ m}}$$

